# GENERALIZED ALPHA GENERALIZED CLOSED SETS IN BITOPOLOGICAL SPACES

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#### **ABSTRACT**

In this paper, we introduce generalized alpha generalized closed sets ( $g\alpha g$  - closed sets) in bitopological spaces and basic properties of these sets are analyzed. Further we define and study  $g\alpha g$  - continuous mappings in bitopological spaces and some of their properties have been investigated.

**Keywords:** Bitopological space, ij -  $g\alpha g$  - closed set, ij -  $g\alpha g$  - open set, ij -  $T_{g\alpha g}$  - space, ij -  $g\alpha g$  - continuous mappings.

## 1. INTRODUCTION

A triple  $(X, \tau_1, \tau_2)$ , where X is a non empty set and  $\tau_1, \tau_2$  are topologies on X is called a bitopological space and J. C. Kelly [2] initiated the study of such spaces . In 1990, M. Jelic [3] introduced the concepts of alpha open sets in bitopological spaces. In 1986, T. Fukutake [6] introduced the concepts of generalized closed sets in bitopological spaces and after that several authors turned their attention towards generalizations of various concepts of topology by considering bitopological spaces. O. A. El-Tantawy and H. M. Abu-Donia [5] introduced alpha generalized closed sets in bitopological spaces. In 2012, V. Seenivasan and S. Kalaiselvi [7] introduced and studied the concepts of generalized semi generalized closed sets in bitopological spaces.

The purpose of this paper is to introduce a new class of closed sets called generalized alpha generalized closed sets ( $g\alpha g$ -closed sets) and generalized alpha generalized continuous mappings ( $g\alpha g$  - continuous mappings) in bitopological spaces and investigate some of their properties .

## 2. PRELIMINARIES

Throughout this paper X, Y and Z always represent non empty bitopological spaces  $(X, \tau_1, \tau_2)$ ,  $(Y, \sigma_1, \sigma_2)$  and  $(Z, \rho_1, \rho_2)$  on which no separation axioms are assumed unless explicitly mentioned and the integers  $i, j, k \in \{1,2\}$ .

For a subset A of X  $\tau_i$  - cl(A) (resp.  $\tau_i$  - int(A),  $\tau_i$  -  $\alpha cl(A)$ ) denote the closure (resp. interior,  $\alpha$  - closure) of A with respect to the topology  $\tau_i$ . By (i,j) we mean the pair of topologies  $(\tau_i,\tau_i)$ .

**Definition: 2.1** A subset *A* of a bitopological space  $(X, \tau_1, \tau_2)$  is called

(i)  $ij - \alpha$  - open [3] if  $A \subseteq \tau_i$  -  $int(\tau_i - cl(\tau_i - int(A)))$ , where  $i \neq j; i, j = 1, 2$ .

(ii)  $ij - \alpha$  - closed [3] if X - A is  $ij - \alpha$  - open, where  $i \neq j$ ; i, j = 1, 2.

Equivalently, a subset A of a bitopological space  $(X, \tau_1, \tau_2)$  is called  $ij - \alpha$  - closed if  $\tau_i - cl(\tau_i - \operatorname{int}(\tau_i - cl(A))) \subseteq A$ .

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**Definition: 2.2** A subset A of a bitopological space  $(X, \tau_1, \tau_2)$  is called

- (i) ij generalized closed (briefly ij g closed) [6] if  $\tau_i$   $cl(A) \subseteq U$  whenever  $A \subseteq U$  and U is  $\tau_i$  open in X.
- (ii) ij generalized open (briefly ij g -open) [6] if X A is ij g -closed.
- (iii)  $ij \alpha$  generalized closed (briefly  $ij \alpha g$  closed) [5] if  $\tau_i \alpha cl(A) \subseteq U$  whenever  $A \subseteq U$  and U is  $\tau_i$  open in X.
- (iv)  $ij \alpha$  generalized open (briefly  $ij \alpha g$  open) [5] if X A is  $ij \alpha g$  closed.
- (v) ij generalized  $\alpha$  closed (briefly ij  $g\alpha$  -closed) [4] if  $\tau_j$   $\alpha cl(A) \subseteq U$  whenever  $A \subseteq U$  and U is  $\tau_i$   $\alpha$  open in X.
- (vi) ij generalized  $\alpha$  open (briefly ij  $g\alpha$  open) [4] if X A is ij  $g\alpha$  closed.

**Definition: 2.3** A bitopological space  $(X, \tau_1, \tau_2)$  is called  $ij - T_{1/2}$  space [6] if every ij - g -closed set in it is  $\tau_j$  -closed.

**Definition:** 2.4 A map  $f:(X,\tau_1,\tau_2) \to (Y,\sigma_1,\sigma_2)$  is called

- (i)  $\tau_i \sigma_k$  continuous [1] if the inverse image of every  $\sigma_k$  closed in  $(Y, \sigma_1, \sigma_2)$  is  $\tau_i$  closed in  $(X, \tau_1, \tau_2)$ .
- (ii)  $ij g \sigma_k$  continuous [1] if the inverse image of every  $\sigma_k$  closed in  $(Y, \sigma_1, \sigma_2)$  is ij g closed in  $(X, \tau_1, \tau_2)$ .
- (iii)  $ij \alpha g \sigma_k$  continuous if the inverse image of every  $\sigma_k$  closed in  $(Y, \sigma_1, \sigma_2)$  is  $ij \alpha g$  closed in  $(X, \tau_1, \tau_2)$ .
- (iv)  $ij g\alpha \sigma_k$  continuous if the inverse image of every  $\sigma_k$  closed in  $(Y, \sigma_1, \sigma_2)$  is  $ij g\alpha$  closed in  $(X, \tau_1, \tau_2)$ .

#### 3. GENERALIZED ALPHA GENERALIZED CLOSED SETS IN BITOPOLOGICAL SPACE

In this section we introduce the concept of ij -  $g\alpha g$  - closed sets in bitopological spaces and discuss some of the related properties.

**Definition: 3.1** A subset A of a bitopological space  $(X, \tau_1, \tau_2)$  is said to be a ij - generalized alpha generalized closed set (briefly ij -  $g\alpha g$  - closed) if  $\tau_i$  -  $cl(A) \subseteq U$  whenever  $A \subseteq U$  and U is  $\tau_i$  -  $\alpha g$  - open in X.

**Proposition: 3.2** Every  $\tau_i$  - closed set is ij -  $g\alpha g$  - closed set.

**Proof:** Let A be any  $\tau_j$  - closed set and U be any  $\tau_i$  -  $\alpha g$  - open set containing A. Then  $\tau_j$  -  $cl(A) = A \subseteq U$ . Hence A is ij -  $g \alpha g$  - closed set.

The converse of the above proposition is not true as seen from the following example.

**Example: 3.3** Let  $X = \{a, b, c\}$ ,  $\tau_1 = \{X, \phi, \{a\}\}$ , and  $\tau_2 = \{X, \phi, \{a, b\}\}$ . Then  $\{b, c\}$  is  $12 - g\alpha g$  - closed but not  $\tau_2$  -closed.

**Proposition:** 3.4 Every  $ij - g \alpha g$  - closed set is ij - g - closed.

**Proof:** Let A be any  $ij - g\alpha g$  - closed set and U be any  $\tau_i$  - open set containing A. Since every  $\tau_i$  - open is  $\tau_i - \alpha g$  - open set and A is  $ij - g\alpha g$  - closed set, then  $\tau_j$  -  $cl(A) \subseteq U$ . Hence A is ij - g - closed set.

The converse of the above proposition is not true as seen from the following example.

**Example: 3.5** Let  $X = \{a,b,c\}$ ,  $\tau_1 = \{X,\phi,\{a,b\}\}$ , and  $\tau_2 = \{X,\phi,\{a\},\{b\},\{a,b\}\}$ . Then  $\{a,b\}$  is 12 - g - closed but not  $12 - g\alpha g$  - closed.

**Proposition:** 3.6 Every  $ij - g \alpha g$  - closed set is  $ij - \alpha g$  - closed.

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**Proof:** Let A be any ij -  $g\alpha g$  - closed set and U be any  $\tau_i$  - open set containing A. Since every  $\tau_i$  - open is  $\tau_i$  -  $\alpha g$  - open set and A is ij -  $g\alpha g$  - closed set, then  $\tau_i$  -  $\alpha cl(A) \subseteq \tau_i$  -  $cl(A) \subseteq U$ . Hence A is ij -  $\alpha g$  - closed set.

The converse of the above proposition is not true as seen from the following example.

**Example: 3.7** Let  $X = \{a, b, c\}$ ,  $\tau_1 = \{X, \phi, \{a\}\}$  and  $\tau_2 = \{X, \phi, \{a\}, \{b, c\}\}$ . Then  $\{a, b\}$  is  $12 - \alpha g$  - closed but not  $12 - g \alpha g$  - closed.

**Proposition:** 3.8 Every  $ij - g\alpha g$  - closed set is  $ij - g\alpha$  - closed.

**Proof:** Let A be any  $ij - g\alpha g$  - closed set and U be any  $\tau_i - \alpha$  - open set containing A.

Then  $\tau_i - \alpha cl(A) \subseteq \tau_i - cl(A) \subseteq U$ . Hence A is  $ij - g\alpha$  -closed set.

The converse of the above proposition is not true as seen from the following example.

**Example: 3.9** Let  $X = \{a, b, c, d\}$ ,  $\tau_1 = \{X, \phi, \{a, b, c\}\}$ , and  $\tau_2 = \{X, \phi, \{a, d\}, \{a, b, d\}\}$ .

Then  $\{b\}$  is  $12 - g\alpha$  - closed but not  $12 - g\alpha g$  - closed.

**Definition: 3.10** A subset A of a bitopological space  $(X, \tau_1, \tau_2)$  is said to be a ij - generalized alpha generalized open set (briefly ij -  $g\alpha g$  - open) if X - A is ij -  $g\alpha g$  - closed in  $(X, \tau_1, \tau_2)$ .

**Theorem: 3.11** In a bitopological space  $(X, \tau_1, \tau_2)$ 

- (i) Every  $\tau_i$  open set is ij  $g\alpha g$  open set.
- (ii) Every  $ij g\alpha g$  open set is ij g open.
- (iii) Every  $ij g\alpha g$  open set is  $ij \alpha g$  open and  $ij g\alpha$  open.

**Theorem: 3.12** If A and B are  $ij - g\alpha g$  - closed sets in X, then  $A \cup B$  is  $ij - g\alpha g$  - closed.

**Proof:** Let U be any  $\tau_i$  -  $\alpha g$  - open set containing A and B. Then  $A \subseteq U$  and  $B \subseteq U$ . Since A and B are ij -  $g\alpha g$  - closed sets,  $\tau_j$  -  $cl(A) \subseteq U$  and  $\tau_j$  -  $cl(B) \subseteq U$ .

Now,  $\tau_i - cl(A \cup B) = \tau_i - cl(A) \cup \tau_i - cl(B) \subseteq U$  and so  $\tau_i - cl(A \cup B) \subseteq U$ . Hence  $A \cup B$  is  $ij - g\alpha g$  - closed.

**Theorem: 3.13** If a set A is  $ij - g\alpha g$  - closed, then  $\tau_i - cl(A) - A$  contains no non empty  $\tau_i$  - closed set.

**Proof:** Let A be any  $ij - g \alpha g$  -closed and F be a  $\tau_i$  -closed set such that  $F \subseteq \tau_j$  - cl(A) - A. Since A is  $ij - g \alpha g$  -closed, we have  $\tau_j$  -  $cl(A) \subseteq F^c$ . Then  $F \subseteq \tau_j$  -  $cl(A) \cap (\tau_j - cl(A))^c = \emptyset$ . Hence F is empty.

The converse of the above theorem is not true as seen from the following example.

**Example: 3.14** Let  $X = \{a,b,c\}$ ,  $\tau_1 = \{X,\phi,\{c\}\}$ , and  $\tau_2 = \{X,\phi,\{a\},\{a,b\}\}$ . If  $A = \{a\}$ , then  $\tau_2 - cl(A) - A = \{b,c\}$  does not contain non empty  $\tau_1$  - closed set. But  $A = \{a\}$  is not  $12 - g\alpha g$  - closed.

**Theorem: 3.15** A set A is  $ij - g\alpha g$  - closed if and only if  $\tau_i - cl(A) - A$  contains no non empty  $ij - \alpha g$  - closed set.

**Proof:** Let A be any  $ij - g \alpha g$  - closed and D be a  $ij - \alpha g$  - closed set such that  $D \subseteq \tau_i - cl(A) - A$ .

Since A is  $ij - g\alpha g$  - closed, we have  $\tau_j - cl(A) \subseteq D^c$ . Then  $D \subseteq \tau_j - cl(A) \cap (\tau_j - cl(A))^c = \phi$ .

Thus D is empty.

Conversely, suppose that  $\tau_i$  - cl(A) - A contains no non empty ij -  $\alpha g$  - closed set.

Let  $A \subseteq G$  and G is  $ij - \alpha g$  - open. If  $\tau_i - cl(A) \subseteq G$  then  $\tau_i - cl(A) \cap G^c$  is non empty.

Since  $\tau_j$  - cl(A) is closed and  $G^c$  is ij -  $\alpha g$  - closed, we have  $\tau_j$  -  $cl(A) \cap G^c$  is non empty ij -  $\alpha g$  - closed set of  $\tau_j$  - cl(A) - A which is a contradiction. Therefore  $\tau_j$  -  $cl(A) \not\subseteq G$ . Hence A is ij -  $g\alpha g$  - closed.

**Theorem:** 3.16 If a set A is  $ij - g \alpha g$  - closed, then  $\tau_i - cl(\{x\}) \cap A \neq \emptyset$  holds for each  $x \in \tau_i - cl(A)$ .

**Proof:** If  $\tau_i - cl(\{x\}) \cap A = \emptyset$  for some  $x \in \tau_i - cl(A)$ , then  $A \subseteq (\tau_i - cl(\{x\}))^c$ .

Since A is ij -  $g\alpha g$  - closed, we have  $\tau_j$  -  $cl(A) \subseteq (\tau_i - cl(\{x\}))^c$ . This shows that  $x \notin \tau_j$  - cl(A). This contradicts the assumption.

The converse of the above theorem is not true as seen from the following example.

**Example: 3.17** Let  $X = \{a, b, c\}$ ,  $\tau_1 = \{X, \phi, \{a\}\}$ , and  $\tau_2 = \{X, \phi, \{a\}, \{b, c\}\}$ . For a subset  $A = \{a, b\}$  is not a 12 -  $g \alpha g$  - closed set, but  $\tau_1 - cl(\{x\}) \cap A \neq \phi$ , for each  $x \in \tau_2 - cl(A)$ .

**Theorem: 3.18** If A is a ij -  $g\alpha g$  - closed set of  $(X, \tau_1, \tau_2)$  such that  $A \subseteq B \subseteq \tau_j$  - cl(A), then B is also an ij -  $g\alpha g$  - closed of  $(X, \tau_1, \tau_2)$ .

**Proof:** Let U be any  $\tau_i$  -  $\alpha g$  - open set such that  $B \subseteq U$ . As A is ij -  $g\alpha g$  - closed and  $A \subseteq U$ , we have  $\tau_j$  -  $cl(A) \subseteq U$ . Now  $B \subseteq \tau_j$  - cl(A) which gives,  $\tau_j$  -  $cl(B) \subseteq \tau_j$  -  $cl(\tau_j$  -  $cl(A)) = \tau_j$  -  $cl(A) \subseteq U$ . Thus  $\tau_j$  -  $cl(B) \subseteq U$ . Hence B is ij -  $g\alpha g$  - closed.

**Theorem: 3.19** Let  $A \subseteq Y \subseteq X$  and suppose that A is  $ij - g\alpha g$  - closed in X. Then A is  $ij - g\alpha g$  - closed relative to Y.

**Theorem: 3.20** If A is  $\tau_i - \alpha g$  - open and  $ij - g \alpha g$  - closed in X, then A is  $\tau_j$  - closed in X.

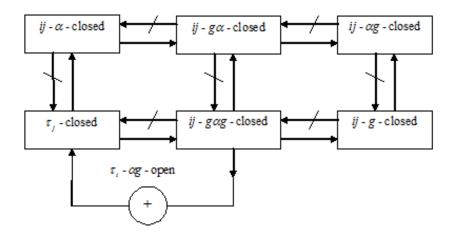
**Proof:** Since A is  $\tau_i$  -  $\alpha g$  - open and ij -  $g\alpha g$  - closed in X, then  $\tau_j$  -  $cl(A) \subseteq A$  and hence A is  $\tau_j$  - closed in X.

**Theorem: 3.21** For each point x of  $(X, \tau_1, \tau_2)$ , either a singleton  $\{x\}$  is  $\tau_i - \alpha g$  - closed or  $\{x\}^c$  is  $ij - g\alpha g$  - closed in X.

**Proof:** If set  $\{x\}$  is not  $\tau_i$  -  $\alpha g$  - closed in X, then  $\{x\}^c$  is not  $\tau_i$  -  $\alpha g$  - open in X and the only  $\tau_i$  -  $\alpha g$  - open set containing  $\{x\}^c$  is the space X itself. Then  $\tau_i$  -  $cl(\{x\}^c) \subseteq X$  and so  $\{x\}^c$  is ij -  $g\alpha g$  - closed in X.

**Theorem: 3.22** If a subset A of  $(X, \tau_1, \tau_2)$  is  $ij - g\alpha g$  - closed in X, then  $\tau_i - cl(A) - A$  is  $ij - g\alpha g$  - open set.

**Remark: 3.23** The following diagram shows the relations among the different types of weakly closed sets that were studied in this section:



## 4. GENERALIZED ALPHA GENERALIZED CONTINUOUS MAPPING

In this section we introduce the concept of ij -  $g\alpha g$  - continuous mapping bitopological spaces and discuss some of the related properties.

**Definition:** 4.1 A mapping  $f:(X,\tau_1,\tau_2) \to (Y,\sigma_1,\sigma_2)$  is said to be  $ij - g\alpha g - \sigma_k$  - continuous if the inverse image of every  $\sigma_k$  - closed in Y is  $ij - g\alpha g$  - closed in X.

**Theorem:** 4.2 If a mapping  $f:(X,\tau_1,\tau_2) \to (Y,\sigma_1,\sigma_2)$  is ij -  $g\alpha g$  -  $\sigma_k$  - continuous, then f is ij -  $\alpha g$  -  $\sigma_k$  - continuous.

**Proof:** Let V be any  $\sigma_k$  - closed in Y. Since f is  $ij - g\alpha g - \sigma_k$  - continuous,  $f^{-1}(V)$  is  $ij - g\alpha g$  - closed in X. Then by proposition (3.6),  $f^{-1}(V)$  is  $ij - \alpha g$  - closed in X. Hence f is  $ij - \alpha g - \sigma_k$  - continuous.

**Theorem:** 4.3 If a mapping  $f:(X,\tau_1,\tau_2)\to (Y,\sigma_1,\sigma_2)$  is  $ij-g\alpha g-\sigma_k$  -continuous, then f is  $ij-g\alpha-\sigma_k$  - continuous.

**Theorem:** 4.4 If a mapping  $f:(X,\tau_1,\tau_2) \to (Y,\sigma_1,\sigma_2)$  is  $ij - g\alpha g - \sigma_k$  - continuous if and only if inverse image of each  $\sigma_k$  - open set of Y is  $ij - g\alpha g$  - open in X.

**Proof:** Let f be  $ij - g\alpha g - \sigma_k$  -continuous. If V is any  $\sigma_k$  -open set of Y then  $V^c$  is  $\sigma_k$  -closed in Y. Since f is  $ij - g\alpha g - \sigma_k$  -continuous,  $f^{-1}(V^c) = (f^{-1}(V))^c$  is  $ij - g\alpha g$  -closed in X. Hence  $f^{-1}(V)$  is  $ij - g\alpha g$  -open in X.

Conversely, let V be any  $\sigma_k$  -closed in Y. By hypothesis  $f^{-1}(V^c)$  is  $ij - g\alpha g$  - open in X. Then  $f^{-1}(V)$  is  $ij - g\alpha g$  - closed in X. Hence f is  $ij - g\alpha g - \sigma_k$  - continuous.

**Theorem:** 4.5 If  $f_1:(X,\tau_1,\tau_2)\to (Y,\sigma_1,\sigma_2)$  is  $ij-g\alpha g-\sigma_k$ -continuous,  $f_2:(Y,\sigma_1,\sigma_2)\to (Z,\rho_1,\rho_2)$  is  $ij-g-\sigma_k$ -continuous and Y is  $ij-T_{1/2}$ -space. Then  $f_2\circ f_1:(X,\tau_1,\tau_2)\to (Z,\rho_1,\rho_2)$  is  $ij-g\alpha g-\sigma_k$ -continuous.

**Proof:** Let V be any  $\rho_k$  -closed in Z. Since  $f_2$  is  $ij - g - \sigma_k$  -continuous and Y is  $ij - T_{1/2}$  -space,  $f_2^{-1}(V)$  is  $\sigma_j$  -closed in Y. Since  $f_1$  is  $ij - g\alpha g - \sigma_k$  -continuous,  $f_1^{-1}(f_2^{-1}(V))$  is  $ij - g\alpha g$  - closed in X. Hence  $f_2 \circ f_1$  is  $ij - g\alpha g - \sigma_k$  -continuous.

**Definition:** 4.6 A bitopological space  $(X, \tau_1, \tau_2)$  is called a ij- $T_{gag}$ -space if every ij- $g\alpha g$ -closed set in it is  $\tau_i$ -closed.

**Proposition: 4.7** Every ij -  $T_{1/2}$ - space is a ij -  $T_{g\alpha g}$  - space.

**Proof:** Let  $(X, \tau_1, \tau_2)$  be a ij -  $T_{1/2}$ - space and let A be a ij -  $g \alpha g$  - closed set in X. By proposition (3.4), A is a ij - g - closed in X. Since X is a ij -  $T_{1/2}$ - space, A is  $\tau_j$  - closed in X. Hence  $(X, \tau_1, \tau_2)$  is a ij -  $T_{g\alpha g}$  - space.

**Theorem:** 4.8 Let  $f:(X,\tau_1,\tau_2) \to (Y,\sigma_1,\sigma_2)$  be a map:

- (i) If  $(X, \tau_1, \tau_2)$  is an  $ij T_{1/2}$  space then f is  $ij g \sigma_k$  continuous if and only if it is  $ij g \alpha g \sigma_k$  continuous.
- (ii) If  $(X, \tau_1, \tau_2)$  is an ij  $T_{g\alpha g}$  space then f is  $\tau_j$   $\sigma_k$  continuous if and only if it is ij  $g\alpha g$   $\sigma_k$  continuous.

## **Proof:**

(i) Let V be any  $\sigma_k$  -closed in Y. Since f is ij - g -  $\sigma_k$  -continuous,  $f^{-1}(V)$  is ij - g -closed in X. By  $(X, \tau_1, \tau_2)$  is an ij -  $T_{1/2}$ - space, which implies,  $f^{-1}(V)$  is  $\tau_j$  -closed. By proposition (3.2),  $f^{-1}(V)$  is ij -  $g\alpha g$  - closed in X. Hence f is ij -  $g\alpha g$  -  $\sigma_k$  - continuous.

Conversely, suppose that f is  $ij - g\alpha g - \sigma_k$  - continuous. Let V be any  $\sigma_k$  - closed in Y.

Then  $f^{-1}(V)$  is  $ij - g \alpha g$  - closed in X. By proposition (3.4),  $f^{-1}(V)$  is ij - g - closed in X. Hence f is  $ij - g - \sigma_k$  - continuous.

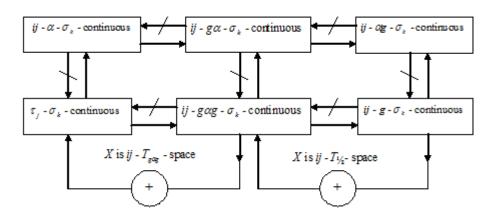
(ii) Let V be any  $\sigma_k$  -closed in Y. Since f is  $\tau_i$  -  $\sigma_k$  - continuous,  $f^{-1}(V)$  is  $\tau_i$  -closed in X.

By proposition (3.2),  $f^{-1}(V)$  is  $ij - g\alpha g$  - closed in X. Hence f is  $ij - g\alpha g - \sigma_k$  - continuous.

Conversely, suppose that f is ij -  $g\alpha g$  -  $\sigma_k$  - continuous. Let V be any  $\sigma_k$  - closed in Y.

Then  $f^{-1}(V)$  is ij -  $g\alpha g$  - closed in X. By  $(X, \tau_1, \tau_2)$  is an ij -  $T_{g\alpha g}$  - space, which implies,  $f^{-1}(V)$  is  $\tau_j$  - closed in X. Hence f is  $\tau_j$  -  $\sigma_k$  - continuous.

**Remark: 4.9** The following diagram shows the relations among the different types of weakly continuous mappings that were studied in this section:



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