



CHARACTERIZATION OF NORMAL
FUZZY SOFT RIGHT NEAR-RING GROUP VIA MAX-NORMS

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ABSTRACT

In this paper, we discuss the notion of max-fuzzy soft N-subgroups by using Molodtsov's definition of soft sets and investigate their related properties with respect to α -inclusion of soft sets.

Keywords: Soft set, fuzzy soft set, Soft N- group, complete, S- fuzzy soft N-group, α -inclusion, Max-norms.

SECTION-1: INTRODUCTION

In 1999, Molodtsov's [10] proposed an approach for modeling, vagueness and uncertainty, called soft set theory. Since its inception, works on soft set theory have been progressing rapidly with a wide-range applications especially in the mean of algebraic structures as in [1-14]. The structures of soft sets, operations of soft sets and some related concepts have been studied by [10-13]. Atagun and Sezgin [3] defined soft N- subgroups and soft N-ideals of an N-group. They studied their properties with respect to soft set operations in more detail. In this paper, the notion of max- fuzzy soft N-subgroups by using Molodtsov's definition of soft sets are discussed and investigate their related properties with respect to α -inclusion of soft sets.

SECTION-2: PRELIMINARIES

This section contains some basic definition and preliminary results which will be needed in the sequel. In what follows let G and S denote a group and max-norm respectively unless otherwise specified.

Definition 2.1: By a near ring, we shall mean an algebraic system $(N, +, \bullet)$, where

- (i) $(N, +)$ forms a group (not necessarily abelian)
- (ii) (N, \bullet) forms a semi group and
- (iii) $(a+b) \bullet c = ac + bc$ for all $a, b \in N$.

Throughout this paper, N will always denote a right near ring whose zero element in O_N . A subgroup M or N write N is contained in M is called a sub near ring of N. For a near ring N, the zero symmetric part of N denoted by N_0 is defined by $N_0 = \{n \in N / nN_0 = O_N\}$

Definition 2.2: Let $(G, +)$ be a group and $A: N \times G \rightarrow G$, $(n, g) \rightarrow ng$, (G, A) is called an N-group if for all $x, y \in N$, for all $g \in G$,

- (i) $x(yg) = (xy)g$ and
- (ii) $(x+y)g = xg + yg$. It is denoted by N^G .

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Clearly, N itself is an N-group by natural operation. A subgroup H of G with N_H contained in H is said to be an N-subgroup of G. Let N be a near-ring and G and ψ two N-groups. Then $f: G \rightarrow \psi$ is called N-homomorphism if for all $g, H \in G$, for all $n \in N$.

- (i) $f(g+H) = f(g) + f(H)$ and
- (ii) $f(ng) = nf(g)$. For all undefined concepts and notions, we refer [17].

From now on, U refers to an initial universe, E is a set of parameters, 2^U is the power set of U and A, B, C is subset of E.

Definition 2.3: Let X be a set. Then a mapping $\mu: X \rightarrow [0, 1]$ is called fuzzy subset of X.

Definition 2.4: Let U be a universal set, E set of parameters and $A \subset E$. Then a pair (δ, A) is called soft set over U, where δ is a mapping from A to 2^U , the power set of U.

Example: Let $X = \{c_1, c_2, c_3\}$ be the set of three cars and $E = \{\text{costly } (e_1), \text{ metallic colour } (e_2), \text{ cheap } (e_3)\}$ be the set of parameters, where $A = \{e_1, e_2\}$ is subset of E. Then

$$(\delta, A) = \{\delta(e_1) = \{c_1, c_2, c_3\}, \delta(e_2) = \{c_1, c_2\}\} \text{ is crisp soft set over } X.$$

Definition 2.5: Let U be a universal set, E set of parameters and A is subset of E. Let $\delta(X)$ denotes the set of all fuzzy subsets of U. Then a pair (δ, A) is called soft set over U, where F is a mapping from A to $\delta(U)$.

Example: Let $U = \{c_1, c_2, c_3\}$ be the set of three cars and $E = \{\text{costly } (e_1), \text{ metallic colour } (e_2), \text{ cheap } (e_3)\}$ be the set of parameters, where $A = \{e_1, e_2\} \subset E$. Then

$$(\delta, A) = \{\delta(e_1) = \{c_1/0.5, c_2/0.6, c_3/0.2\}, \delta(e_2) = \{c_1/0.4, c_2/0.5, c_3/0.7\}\} \text{ is the fuzzy soft set over } U \text{ denoted by } \delta_A.$$

Definition 2.6: Let δ_A be a fuzzy soft set over U and α be a subset of U. Then upper α -inclusion of δ_A denoted by

$$\delta_A^{+\alpha} = \{x \in A / \delta(x) \geq \alpha\} \text{ similarly}$$

$$\delta_A^{-\alpha} = \{x \in A / \delta(x) \leq \alpha\} \text{ is called lower } \alpha\text{-inclusion of } \delta_A.$$

Definition 2.7: A triangular conorm (t-conorm) is a mapping $\max: [0, 1] \times [0, 1] \rightarrow [0, 1]$ that satisfies the following conditions:

- (S1) $\max(x, 0) = x$,
 - (S2) $\max(x, y) = \max(y, x)$,
 - (S3) $\max(x, \max(y, z)) = \max(\max(x, y), z)$,
 - (S4) $\max(x, y) \leq \max(x, z)$ whenever $y \leq z$, for all $x, y, z \in [0, 1]$.
- Replacing 0 by 1 in condition max, we obtain the concept of t-norm min.

Lemma 2.8: Let 'min' be a t-norm. Then t-co norm 'max' can be defined as $\max(x, y) = 1 - \min(1-x, 1-y)$.

Proof: straight forward

Definition 2.9: Let δ_A and Δ_B be fuzzy soft sets over the common universe U and $\psi: A \rightarrow B$ a function. Then fuzzy soft image of δ_A under ψ over U denoted by $\psi(\delta_A)$ is a set-valued function, when $\psi(\delta_A): B \rightarrow 2^U$ defined by

$$\psi(\delta_A)(b) = \begin{cases} \max\{\delta(a) / a \in A \text{ and } \psi(a) = b\}, & \text{if } \psi^{-1}(b) \neq \Phi \\ \Phi & \text{otherwise} \end{cases} \text{ for all } b \in B.$$

The fuzzy soft pre image of Δ_B under ψ over U, denoted by $\psi^{-1}(\Delta_B)$ is a set valued function where $\psi^{-1}(\Delta_B): A \rightarrow 2^U$ defined by $\psi^{-1}(\Delta_B)(b) = G(\psi(a))$ for all $a \in A$. Then fuzzy soft anti image of δ_A under Δ over U denoted by $\psi^*(\delta_A)$ is a set valued function, where

$$\psi^*(\delta) = \begin{cases} \min\{\delta(a) / a \in A \text{ and } \psi(a) = b\}, & \text{if } \psi^{-1}(b) \neq \Phi \\ \Phi & \text{otherwise} \end{cases} \text{ for all } b \in B.$$

Definition 2.10: Let H be an N-subgroup of G and δ_H be a fuzzy soft set over G. If for all $x, y \in H$ and $n \in N$,

- (i) $\delta_H(x-y) \geq \min\{\delta_H(x), \delta_H(y)\}$ and
- (ii) $\delta_H(nx) \geq \delta_H(x)$, then the fuzzy soft set F_H is called a fuzzy soft N-subgroup of G.

Definition 2.11: Let H be an N-subgroup of G and F_H be a fuzzy soft set over G. If for all $x, y \in H$ and $n \in N$,

- (i) $\delta_H(x-y) \leq \max\{\delta_H(x), \delta_H(y)\}$ and
- (ii) $\delta_H(nx) \leq \delta_H(x)$, then the fuzzy soft set δ_H is called max-fuzzy soft N-subgroup of G.
It is denoted by $\delta_{H \triangleleft_N} G$

Example: Consider $N = \{0, 1, 2, 3\}$ be a near-ring with operations $+$ and \bullet

| | | | | |
|---|---|---|---|---|
| + | 0 | 1 | 2 | 3 |
| 0 | 0 | 1 | 2 | 3 |
| 1 | 1 | 2 | 3 | 0 |
| 2 | 2 | 3 | 0 | 1 |
| 3 | 3 | 0 | 1 | 2 |

| | | | | |
|-----------|---|---|---|---|
| \bullet | 0 | 1 | 2 | 3 |
| 0 | 0 | 0 | 0 | 0 |
| 1 | 0 | 1 | 2 | 3 |
| 2 | 0 | 2 | 1 | 2 |
| 3 | 0 | 3 | 2 | 1 |

Let $G = N$, $H = \{0, 2\} \triangleleft_N G$ and F_H be a fuzzy soft set over G , where $\delta: H \rightarrow 2^G$ is a set valued function defined by $\delta(x) = \{0\} \cup \{y \in G / 3x=y\}$ for $x \in H$. Then $\delta(0) = \{0\}$ and $\delta(2) = \{0,2\}$. Therefore $\delta_H \triangleleft_N G$. If we define a fuzzy soft set Δ_H over G by $\Delta(x) = \{y \in G / 3x = y\}$ for all $x \in H$. Then $\Delta(0) = \{0\}$ and $\Delta(2) = \{2\}$. since $\Delta(2-2) = \Delta(0)$ not in $\Delta(2)$. Δ_H is not a max- fuzzy soft N -subgroup of G .

Definition 2.12: The relative complement of the fuzzy soft set δ_A over G is denoted by δ_A^r , where $\delta_A^r: A \rightarrow 2^U$ is a mapping given as $\delta_A^r(x) = G / \delta_A(x)$, for all $x \in A$.

SECTION-3: Properties of max- fuzzy soft N -subgroup

Proposition 3.1: Let δ_H be a fuzzy soft set over G and α be a subset of G . If δ_H is max- fuzzy soft N -subgroup of G , then lower α -inclusion of δ_H is an N -subgroup of G .

Proof: since δ_H is max- fuzzy soft N -subgroup of G . Assume $x, y \in H$

Let $\delta_H^{-\alpha}$ and $n \in N$, then $\delta_H(x) \leq \alpha$ and $\delta_H(y) \leq \alpha$. We need to show that $x-y \in \delta_H^{-\alpha}$ and $n \in \delta_H^{-\alpha}$. Since δ_H is max- fuzzy soft N -subgroup of G , it follows that $\delta_H(x-y) \leq \max \{\delta_H(x), \delta_H(y)\} \leq \max \{\alpha, \alpha\} \leq \alpha$ and $\delta_H(nx) \leq \delta_H(x) \leq \alpha$ which completes the proof.

Proposition 3.2: Let δ_H be a fuzzy soft set over G and α be a subset of G . If δ_H is fuzzy soft N -subgroup of G , then upper α -inclusion of δ_H is an N -subgroup of G .

Proof: since δ_H is fuzzy soft N -subgroup of G .

Assume $x, y \in \delta_H^{+\alpha}$ and $n \in N$, then $\delta_H(x) \geq \alpha$ and $\delta_H(y) \geq \alpha$. We need to show that $x-y \in \delta_H^{+\alpha}$ and $n \in \delta_H^{+\alpha}$. Since δ_H is fuzzy soft N -subgroup of G , it follows that $\delta_H(x-y) \geq \min \{\delta_H(x), \delta_H(y)\} \geq \min \{\alpha, \alpha\} \geq \alpha$ and $\delta_H(nx) \geq \delta_H(x) \geq \alpha$ which completes the proof.

Proposition 3.3: Let δ_H be a fuzzy soft set over G . Then δ_H is max- fuzzy soft N - subgroup of G if δ_H^r is min-fuzzy soft N -subgroup of G .

Proof: Let δ_H be a max- fuzzy soft N -subgroup of G , then, for all $x, y \in H$ and $n \in N$.

$$\delta_H^r(x-y) = G / \delta_H(x-y) \geq (G / \max\{\delta_H(x), \delta_H(y)\}) = \min\{(G / \delta_H(x)), (G / \delta_H(y))\} = \min\{\delta_H^r(x), \delta_H^r(y)\}$$

$$\delta_H^r(nx) = G / \delta_H(nx) \geq (G / \delta_H(x)) = \delta_H^r(x)$$

δ_H^r is fuzzy soft N -subgroup of G .

Proposition 3.4: Let $\delta_H: X \rightarrow X^1$ be a soft homomorphism of N -subgroups. If δ_H^f is max- fuzzy soft N -subgroups of X , then δ_H is max- fuzzy soft N -subgroup of X^1 .

Proof: Suppose δ_H is max- fuzzy soft N -subgroups of X^1 , then

- (i) Let $x^1, y^1 \in X^1$, there exists $x, y \in X$ such that $f(x) = x^1$ and $f(y) = y^1$. We have $\delta_H(x^1-y^1) = \delta_H(f(x)-f(y)) \leq \max \{\delta_H(x), \delta_H(y)\} = \max \{\delta_H^f(x), \delta_H^f(y)\}$ and

(ii) $\delta_H(nx^1) = \delta_H(nf(x)) \leq \delta_H(f(x)) = \delta_H^f(x)$.
 Therefore δ_H is max- fuzzy soft N-subgroups of X^1 .

Proposition 3.5: Let δ_H be max- fuzzy soft N-subgroups of X and δ_H^* be a fuzzy soft in X given by $\delta_H^*(x) = \delta_H(x) + 1 - \delta_H(1)$ for all $x \in X$. Then F_H^* is max- fuzzy soft N-subgroups of X and $\delta_H \subset \delta_H^*$.

Proof: Since δ_H is max- fuzzy soft N-subgroups of X and $\delta_H^*(x) = \delta_H(x) + 1 - \delta_H(1)$ for all $x \in X$. For any $x, y \in X$, we have $\delta_H^*(1) = \delta_H(1) + 1 - \delta_H(1) = 1 > \delta_H^*(x)$ and

(i) For all $x, y \in X$, we have

$$\begin{aligned} \delta_H^*(x-y) &= \delta_H(x-y) + 1 - \delta_H(1) \\ &\leq \max\{\delta_H(x), \delta_H(y)\} + 1 - \delta_H(1) \\ &= \max\{\delta_H(x) + 1 - \delta_H(1), \delta_H(y) + 1 - \delta_H(1)\} \\ &= \max\{\delta_H^*(x), \delta_H^*(y)\} \end{aligned}$$

(ii) $\delta_H^*(nx) = \delta_H(nx) + 1 - \delta_H(1)$
 $\leq \delta_H(x) + 1 - \delta_H(1) = \delta_H^*(x)$

Therefore δ_H^* is max- fuzzy soft N-subgroup of X and δ_H is subset of δ_H^* .

Proposition 3.6: Let δ_H and δ_Δ be fuzzy soft sets over G . where H and Δ are N-subgroups of G and $\psi: H \rightarrow \Delta$ is an N-homomorphism. If δ_H is max - fuzzy N-subgroups of G , then so is $\psi(\delta_H)$.

Proof: Let $\alpha_1, \alpha_2 \in \Delta$ such ψ is surjective, there exists $a_1, a_2 \in H$ such that $\psi(a_1) = \alpha_1$ and $\psi(a_2) = \alpha_2$. Thus

$$\begin{aligned} \Psi(\delta_H)(x) &= \max\{\delta(H) / H \in H, \psi(H) = \alpha_1 - \alpha_2\} \\ &= \max\{\delta(H) / H \in H, H = \psi^{-1}(\alpha_1 - \alpha_2)\} \\ &= \max\{\delta(H) / H \in H, H = \psi^{-1}(\psi(\alpha_1 - \alpha_2)) = A_1 - A_2\} \\ &= \max\{\delta(a_1 - a_2) / \alpha_1, \alpha_2 \in \Delta, \psi(H_i) = \alpha_i, i = 1, 2\} \\ &= \max\{(\max\{\delta(a_1) / \alpha_1 \in \Delta, \psi(H_1) = \alpha_1\}), (\max\{\delta(a_2) / \alpha_2 \in \Delta, \psi(H_2) = \alpha_2\})\} \\ &= \max\{\psi(\delta_H)(a_1), \psi(\delta_H)(a_2)\} \end{aligned}$$

Now let $n \in \mathbb{N}$ and $\alpha \in \Delta$. Since ψ is surjective, there exists $H \in H$ such that $\psi(H) = \alpha$

$$\begin{aligned} \psi(\delta_H)(n\alpha) &= \max\{\delta(H) / H \in H, \psi(H) = n\alpha\} \\ &= \max\{\delta(H) / H \in H, H = \psi^{-1}(n\alpha)\} \\ &= \max\{\delta(H) / H \in H, H = \psi^{-1}(n\psi(H))\} \\ &= \max\{\delta(H) / H \in H, H = \psi^{-1}(\psi(nH)) = nH\} \\ &= \max\{\delta(nH) / H \in H, H = \psi^{-1}(H) = \alpha\} \\ &= \max\{\delta(H) / H \in H, H = \psi^{-1}(H) = \alpha\} \\ &= \psi(\delta_H)(\alpha) \end{aligned}$$

$\psi(\delta_H)$ is max - fuzzy soft N-subgroup of G .

Proposition 3.7: Let $\delta_H: X \rightarrow Y$ be a soft homomorphism of N-subgroups. If δ_H is max - fuzzy soft N-subgroups of Y , then δ_H^f is max - fuzzy soft N-subgroups of X .

Proof: Suppose δ_H is max - fuzzy soft N-subgroups of Y , then

For all $x, y \in X$, we have

$\delta_H^f(x-y) = \delta_H(f(x) - f(y)) \leq \max\{\delta_H(f(x)), \delta_H(f(y))\} = \max\{\delta_H^f(x), \delta_H^f(y)\}$ and
 (i) $\delta_H^f(nx) = \delta_H(nf(x)) \leq \delta_H(f(x)) = \delta_H^f(x)$.
 Therefore δ_H^f is max- fuzzy soft N-subgroups of Y .

Proposition 3.8: Let δ_H and δ_Δ be fuzzy soft sets over G , where H and Δ are N-subgroups of G and ψ be an N-homomorphism from H to Δ . If δ_Δ is max - fuzzy soft N- subgroups of G , then so is $\psi^{-1}(\delta_\Delta)$.

Proof: Let $a_1, a_2 \in H$, then

$$\begin{aligned} \psi^{-1}(\delta_\Delta)(a_1 - a_2) &= \delta(\psi(a_1 - a_2)) \\ &\leq \max\{\delta(\psi(a_1)), \delta(\psi(a_2))\} \\ &\leq \max\{\psi^{-1}(\delta_\Delta)(a_1), \psi^{-1}(\delta_\Delta)(a_2)\} \end{aligned}$$

Now let $n \in \mathbb{N}$ and $H \in H$, then

$$\psi^{-1}(\delta_\Delta)(nH) = \delta(\psi(nH)) = \delta(n\psi(H)) = G(\psi(H)) = \psi^{-1}(\delta_\Delta)(H)$$

Therefore $\psi^{-1}(\delta_\Delta)$ is max - fuzzy soft N-subgroups of G .

Proposition 3.9: A fuzzy soft subset δ_H of G is min- fuzzy soft N-subgroups of G . if and only if δ_H^c is max - fuzzy soft N-subgroups of G .

Proof: Let δ_H be a min- fuzzy soft N-subgroups of G . For all $x, y \in G$, we have

$$\begin{aligned} \text{(i)} \quad \delta_H^c(x-y) &= 1 - \delta_H(x-y) \\ &\leq 1 - \min(\delta_H(x), \delta_H(y)) \\ &= 1 - \min(1 - \delta_H^c(x), 1 - \delta_H^c(y)) \\ &= \max(\delta_H^c(x), \delta_H^c(y)) \end{aligned}$$

$$\begin{aligned} \text{(ii)} \quad \delta_H^c(nx) &= 1 - \delta_H(nx) \\ &\leq 1 - \delta_H(x) = \delta_H^c(x) \end{aligned}$$

δ_H^c is max - fuzzy soft N-subgroups of G .

Proposition 3.10: If δ_H and δ_Δ be two max -fuzzy soft N-subgroups of G , then $\delta_H \cup \delta_\Delta$ also max -fuzzy soft N-subgroup of G

Proof: Since H and Δ are N-subgroup of G , then $H \cap \Delta$ is an N-subgroup of G .

Let $P = \delta_H \cup \delta_\Delta$, where $P(x) = \delta_H(x) \cup \delta_\Delta(x)$ for all $x \in H \cap \Delta$ not equal to empty. Then for all $x, y \in H \cap \Delta$ and $n \in N$,

$$\begin{aligned} P(x-y) &= \delta_H(x-y) \cup \delta_\Delta(x-y) \\ &\leq \max \{ \max \{ \delta_H(x), \delta_H(y) \}, \max \{ \delta_\Delta(x), \delta_\Delta(y) \} \} \\ &= \max \{ \max \{ \delta_H(x), \delta_\Delta(x) \}, \max \{ \delta_H(y), \delta_\Delta(y) \} \} \\ &= \max \{ P(x), P(y) \} \end{aligned}$$

$$\begin{aligned} P(nx) &= \delta_H(nx) \cup \delta_\Delta(nx) \\ &\leq \max \{ \delta_H(x), \delta_\Delta(x) \} \\ &= P(x) \end{aligned}$$

Therefore $\delta_H \cup \delta_\Delta$ also max -fuzzy soft N-subgroup of G .

Definition 3.1: A max -fuzzy soft N-subgroup FH of G is said to be complete if it is normal and there exists $x \in X$ such that $\delta_H(z) = 0$.

Proposition 3.11: Let δ_H be max -fuzzy soft N-subgroup of G and let w be a fixed element of G such that $\delta_H(1) = \delta_H(w)$. Define a fuzzy soft set δ_H^* in G by $\delta_H^*(x) = \delta_H(x) - \delta_H(w) / \delta_H(1) - \delta_H(w)$ for all $x \in G$. Then δ_H^* is complete max -fuzzy soft N-subgroup of G .

Proof: For any $x, y \in G$, we have

$$\begin{aligned} \delta_H^*(x-y) &= \delta_H(x-y) - \delta_H(w) / \delta_H(1) - \delta_H(w) \\ &\leq \max \{ \delta_H(x), \delta_H(y) \} - \delta_H(w) / \delta_H(1) - \delta_H(w) \\ &= \max \{ \{ \delta_H(x), \delta_H(y) \} - \delta_H(w) / \delta_H(1) - \delta_H(w), \{ \delta_H(x), \delta_H(y) \} - \delta_H(w) / \delta_H(1) - \delta_H(w) \} \\ &= \max \{ \delta_H^*(x), \delta_H^*(y) \} \end{aligned}$$

$$\begin{aligned} \delta_H^*(nx) &= \delta_H(nx) - \delta_H(w) / \delta_H(1) - \delta_H(w) \\ &\leq \delta_H(x) - \delta_H(w) / \delta_H(1) - \delta_H(w) \\ &= \delta_H^*(x) \end{aligned}$$

Therefore δ_H^* is an complete max -fuzzy soft N-subgroup of G .

CONCLUSION

This paper summarized the basic concepts of fuzzy soft sets. By using these concepts, we studied the algebraic properties of max- fuzzy soft N-subgroups. This work focused on fuzzy pre-image, fuzzy soft image, fuzzy soft anti-image.

FUTURE WORK

To extend this work, one could study the properties of min-fuzzy soft N-subgroups in other algebraic structures such as rings and fields.

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